

Algorithms and Data Structures

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Where innovation starts

Content

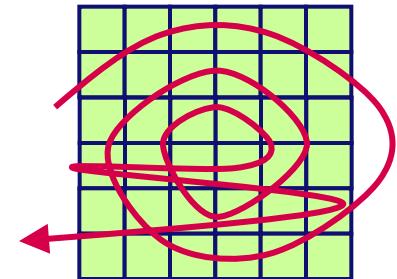
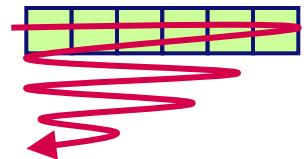
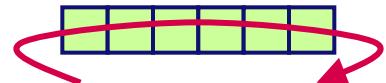
- General principles
- Searching
- Sorting
- Optimising (more algorithms and data structures)

General principles

- Data structures
 - built from variables, arrays, objects referring to each other
- Algorithms
 - built from if, if-else, for, while, functions calling each other
- To be designed together
 - like the railway topology and the train schedule
 - you cannot design an efficient train schedule
 - unless you know the railway topology

General principles (continued)

- Searching
 - one-dimensional problems
 - with single-loop solutions
- Sorting
 - one-dimensional problems
 - with nested-loop solutions
 - useful to prepare for easy searching
- Optimising
 - two-dimensional problems
 - with complex nested-loop solutions
 - good example: shortest path problems
 - useful in route planners and internet packet routing



General principles (continued)

- Issues
 - correctness
 - efficiency
- Correctness
 - respecting array bounds
 - not using null pointers
 - initialising all variables
 - careful reasoning
- Efficiency
 - data structures for memoization
 - $\mathcal{O}(n)$ is better than $\mathcal{O}(n^2)$ and $\mathcal{O}(n^3)$
 - sometimes one has to accept $\mathcal{O}(e^n)$
 - use existing classics

Searching

- Basic idea
 - data in one array
 - scan the entire array with one for-loop
- Basic code

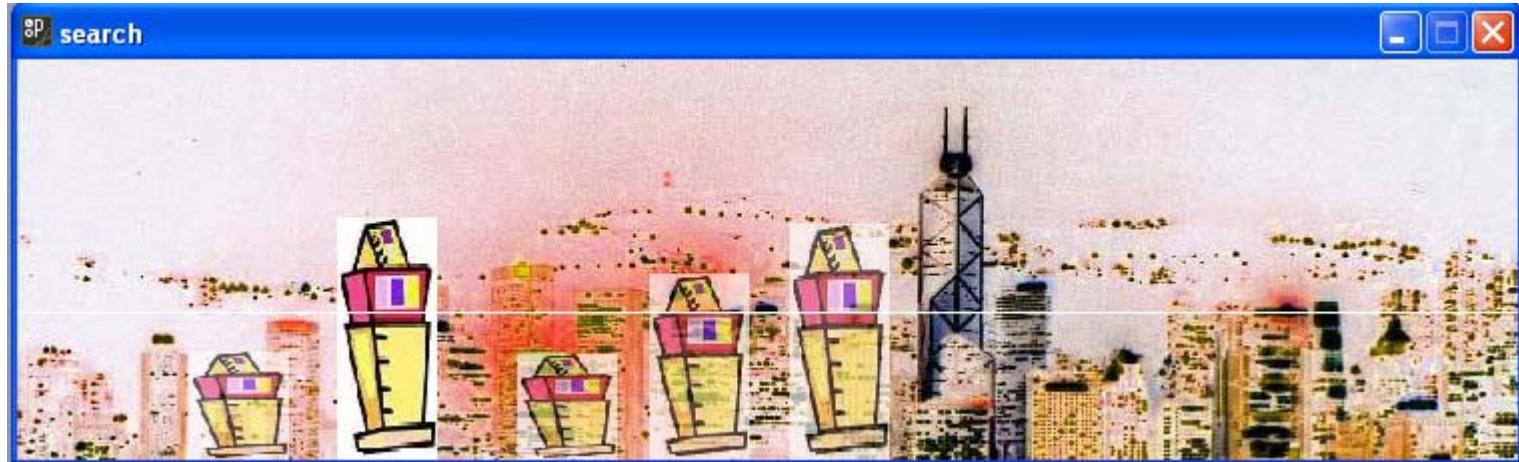
```
int[] a=new int[N];
// a is filled here
for (int i=0; i<N; i++) {
    if (a[i] == x) {
        // aha, x found
    }
}
```

Searching

- Tricks of the trade
 - for an array of N elements
 - the indexes run from 0 to N-1
 - use a local loop counter named i, j or k
 - use a boolean found to stop once your x is found
 - use the pseudo value infinity to begin a min or max loop

Searching

- Demo application
 - edit an array of towers
 - random height levels
 - calculate average
 - find the tallest



Searching

- Interface of the demo

```
void keyPressed() {  
    if(keyCode == LEFT) { x=x-2; }  
    if(keyCode == RIGHT) { x=x+2; }  
    if(key == ' ') { // add tower  
        if (towers<maxtowers){  
            loc[towers]=x;  
            lvl[towers]=floor(random(0,200));  
            towers++;  
        }  
        if(keyCode == ENTER) { done=true; }  
    }  
}
```

For each tower index there is a location loc and a height level lvl

The construction truck is at horizontal position x

Searching

- Action of the demo

```
// in draw
if (done) {
    int i=tallest();
    tint(255,255);
    image(tower,loc[i],200-lvl[i],50,lvl[i]);
    int a=average();
    stroke(255);
    line(0, 200-a, 750, 200-a);
}
```

Finding a maximum

Calculating an average

Searching

- Finding a maximum

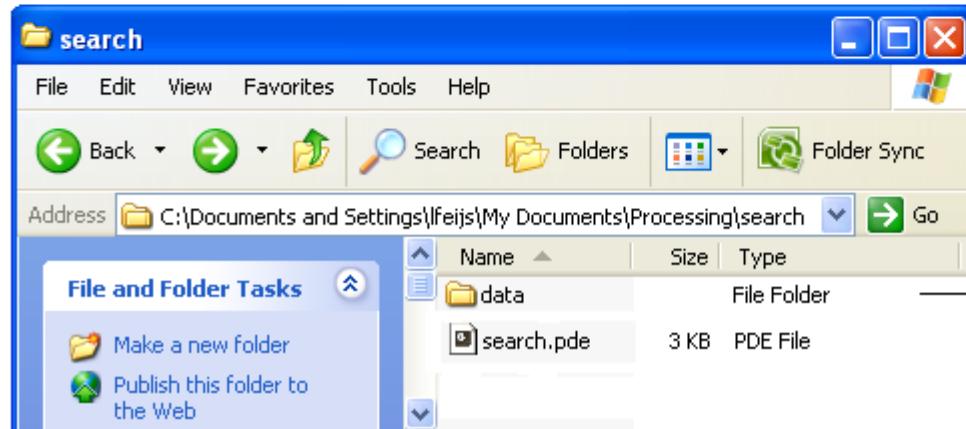
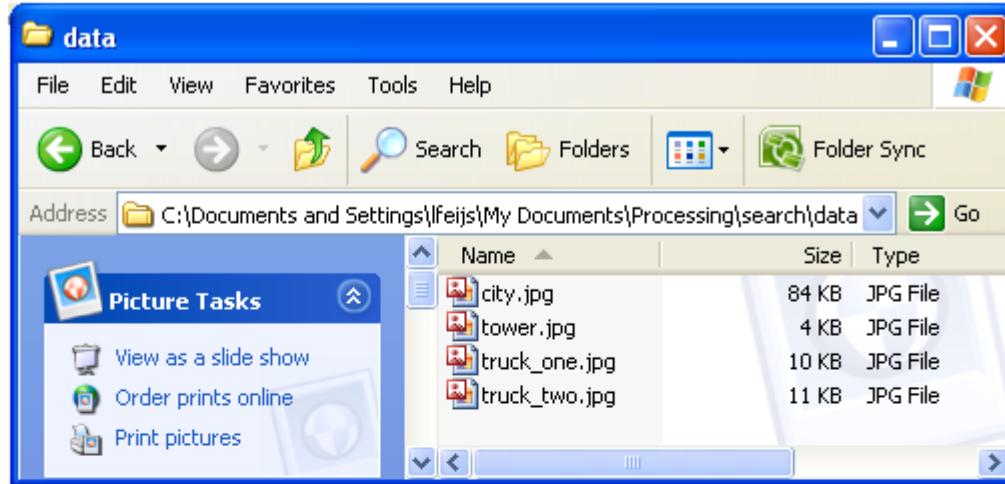
```
int tallest() {  
    int m=-1; // max level found so far  
    int i=-1; // index where it's found  
    for (int j=0; j<towers; j++)  
        if (lvl[j] > m) {  
            m = lvl[j];  
            i = j;  
        }  
    return i;  
}
```

Searching

- Calculating an average

```
int average() {  
    int s=0; // sum calculated so far  
    for (int j=0; j<towers; j++)  
        s = s+lvl[j];  
    if (towers>0)  
        return s / towers;  
    else return 1;  
}
```

Searching (more about the demo)



Exercises on searching

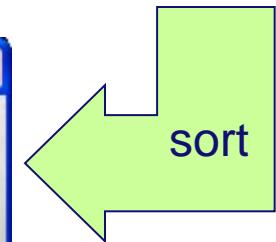
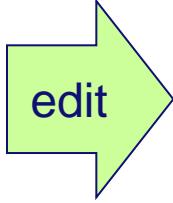
- Do it yourself
 - find the lowest tower
- Food for thought
 - can you find the median?

Sorting

- Demo application
 - edit an array of towers
 - three tower types
 - towers as objects
 - sort by level



Sorting



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Sorting

- Selection sort
 - noted for its simplicity
 - see e.g. (Dutch) wikipedia, selection sort
 - more: heapsort, insertion sort, bubble sort, quicksort, Shellsort, ...

```
// invoer = array met integers
for (int i = 0; i < array.length; i++) {

    // zoek kleinste in de rest van de array
    int minIndex = i;
    for (int j = i; j < array.length; j++) {
        if (array[j] < array[minIndex]) {
            minIndex = j;
        }
    }

    // verwissel waarden
    int temp = array[i];
    array[i] = array[minIndex];
    array[minIndex] = temp;
}
```

Sorting

```
void selectionSort() {
    for (int i = 0; i < towers; i++) {
        // when here: i smallest values are sorted in 0..i-1
        int mi = i;
        for (int j = i; j < towers; j++) {
            // when here: mi is index of smallest in i..j-1
            if (twr[j].lvl < twr[mi].lvl)
                mi = j;
        }
        // swap towers at indexes i and mi
        Tower tmp = twr[i]; twr[i] = twr[mi]; twr[mi] = tmp;
    }
}
```

Sorting (oo)

- Object orientation

- instead of 3 arrays of single tower-attributes

```
int[] loc = new int[maxtowers]; // location, i.e. x value  
int[] lvl = new int[maxtowers]; // level, i.e. height  
int[] typ = new int[maxtowers]; // type, either 0,1, or
```

- define one array of tower objects with 3 attributes each

```
class Tower {  
    int loc; // location, i.e. x value  
    int lvl; // level, i.e. height  
    int typ; // type, either 0,1, or 2  
    // etc.  
}  
Tower[] twr = new Tower[maxtowers];
```

Exercises on sorting

- Study and run the sorting demo
- Do it yourself
 - bubble sort
 - e.g. read wikipedia: bubble sort
- Food for thought
 - now can you find the median?